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# THEORETICAL AND NUMERICAL INVESTIGATION OF POLYMER-PARTICLE NANOCOMPOSITES AND THEIR EFFECTIVE MATERIALS PROPERTIES

Final Technical Report

AFOSR (FA9550-08-1-0107),

(Dec. 1, 2007-Nov. 11, 2008)

Qi Wang Department of Mathematics Florida State University Tallahassee, FL 32312

#### **Abstract**

Polymer particulate nanocomposites (PNCs) have many industrial and military applications. They can achieve very high mechanical modulus and possess superior transport or barrier properties. The project aimed to study the mesoscopic structure formation during flow processing and the corresponding rheological consequence leading to characterization of material properties in solid states. Significant progress has been made to model the materials and to understand their rheological properties in melt or solution processing during the project year. In addition, the anisotropic molecular configuration in bent-core liquid crystals and its impact to the macroscopic material properties are investigated; applications of the modeling and numerical tools developed for complex fluids are used to important biological applications.

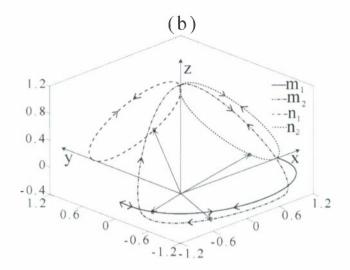
The objective of the project is to develop a suite of multiscale models and simulation tools to probe the flowing and solid-state properties of liquid crystal polymer (LCP) and polymer nano-particle (anisotropic particle in particular) composite (PNC) materials guided by Air Force contact Dr. Richard Vaia of material directorate WPAFB. The grant began on December 1, 2007 and ended on Nov. 30, 2008 due to my transfer from Florida State University to University of South Carolina. The research activities included developing kinetic theories for blends of rigid liquid crystal polymers and flexible polymers as well as theories for biaxial liquid crystals and nano-particle dispersions; multiphase flows of rigid LCPs in viscous or polymeric matrices; application of the complex fluids theories and simulation tools to biological settings like biofilm modeling and simulation. In the following, I summarize the completed work and list the publications and synergistic activities during the period. For more technical details, please refer to our publications.

#### Structure formation and defect evolution in shear flows of liquid crystal polymers

The Pi and his collaborators (M. G. Forest, and X Yang of UNC-CH) continued the refined analysis on the extended Doi-Hess kinetic theory for shear flows of inhomogeneous liquid crystal polymers. The aim here is to provide a comprehensive understanding of the poly-domain flow behavior as well as the mesoscale structures governed by the kinetic theory and closure models for inhomogeneous LCPs. We focused on multidimensional phenomena where the defect formation and annihilation dominates the mesoscale morphology leading to the experimentally observed optical turbulence. A spatially 2-D tensor based solver is developed to study the multiscale phenomena. Following the monodomain road map, we have identified a variety of temporal-spatial structures and patterns in sheared nematic LCPs of inhomogeneous flows. A new diagnostic is developed to detect and monitor the defect dynamics in time and space. Various spatial-temporal phenomena in the sheared nematic system are explored and reported, improving one's understanding of defect dynamics and their rheological and fluid mechanics consequence.

#### Multiscale kinetic theories for flows of biaxial liquid crystal polymers

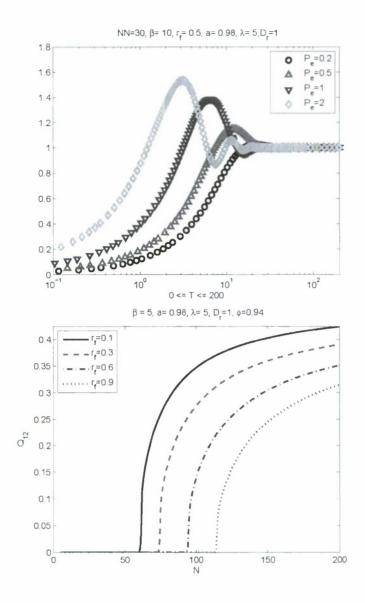
Given the rising interests in the modeling of nanofluids of biaxial constituents such as the bent-core liquid crystal polymers, my graduate student Sarthok Sircar and I developed hydrodynamic theories for the biaxial liquid crystal polymer by modeling it as an ellipsoid or a V-shaped rigid body suspended in viscous solvent. The excluded volume interaction potential is calculated from the first principle. The probability density function is sought by a spectral method for the Smoluchowski equation based on the Wigner function expansion. Lower-dimensional approximation to the second moment space or reduced order models is also attempted to resolve the coarse-scale dynamics. We have studied the flow-induced structure transition with a general excluded volume potential and the monodomain structure in sheared biaxial liquid crystals. In the case ellipsoidal biaxial lcps, two time-periodic motions are identified along with the chaotic motion. While the chaotic motion is apparently absent in the bent-core liquid crystal system in steady shear. The picture below shows one of the time-periodic motion observed in sheared ellipsoidal and bent-core biaxial LCPs, called fluttering motion.



#### Kinetic theories and rheological prediction for polymer nano-particle composites

The PI along with his collaborators have developed a new set of kinetic theories for polymer nano-particle composites accounting for the semiflexibility of the nano-particles such as nanoclays, silicones, etc. as well as the contact interaction between flexible polymers and the nano-particles. These nano-particles can be semiflexible rods or thin platelets. The effect of the semiflexibility and surface contact interaction between the nanoparticle and the host polymer matrix influences the equilibrium phase as well as the shear flow induced phase significantly. The first figure below depicts the shear viscosity prediction at a set of selected shear rates. The prediction qualitatively matches the experimental data.

In the next figure, the semiflexibility of the "nanoparticles" or inclusions also affects the phase behavior of the nanocomposites, where  $r_f$  denotes the degree of semiflexibility of the nanoparticles (r=0 corresponds to the fully rigid limit). The details are summarized in two papers either accepted or submitted.

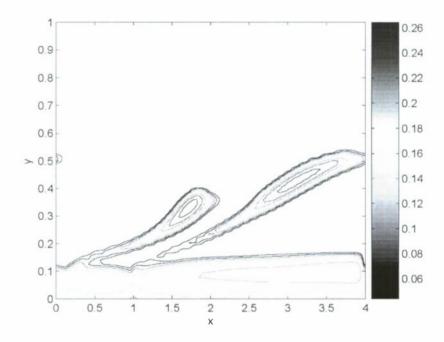


#### Modeling blends of liquid crystal polymers and flexible polymers

In collaboration with Prof. Ping Lin of National University of Singapore, we are conducting a series studies on the blends of immiscible liquid crystal polymers and viscous fluids or flexible polymer fluids. Various combinations of the constitutive models for the flexible polymers can be incorporated into the phase-field model for the blends. The goal is to understand the motion of liquid crystal droplets in viscoelastic matrix subject to external shear or pressure. This study would shed light on the mixing of liquid crystal polymers in polymer matrices through external stirring motion. A finite element solver for the flow problem has been implemented and preliminary numerical results are obtained.

## **Applications to biofilm modeling**

The experience and expertise acquired during our studies of complex fluids, especially, the liquid crystal polymer and flowing nanocomposites has enabled us to model multiphase complex fluids both theoretically and numerically using the phase field approach. We have found applications of our models and methodologies in biofilms, amixtures of polymeric network and viscous fluid components comprising of bacteria and nutrient-rich solvent, cell motility, etc. The 2-D and 3-D simulation code have been developed and being paralellized presently. We are applying a coarse-grain dynamical model for semi-flexible polymers to study the self-assembly phenomena in F-actin solution. This could have a potential impact on tissue regeneration for wounded soldiers and fabrication of high performance materials. Figure below depicts the detachment of a biofilm in shear flows in a 2-D simulation.



The research activities on the project funded by the award proceeded smoothly according to the plan. Additional projects closely related to the originally proposed were identified and added to our research activities (like actin self-assembly study and applications to biofilms etc.). The slightly expanded scope of research—facilitated our efforts for the overall objective as well as addressing the need of the Air Force.

#### Personnel Supported through the grant

Mr. Sarthok Sircar

Ph. D candidate, Florida State University, Ph. D. expected

date: May, 2009

Dr. Guanghua Ji

Postdoc Associate, Florida State University

#### **Point of Contact**

Dr. Richard Vaia, AFRL/MLBP, WPAFB, OH, Phone: 937-255-9184. The last time we met was in the contractor's meeting held at WPAFB, Dayton, OH, August, 2008.

#### Papers published and in press during the funded period

- 1. T. Y. Zhang, N. Cogan, and Q. Wang, "Phase Field Models for Biofilms. II. 2-D Numerical Simulations of Biofilm-Flow Interaction," Communications in Computational Physics, 4 (2008), pp. 72-101.
- 2. Xiaofeng Yang, Zhenlu Cui, M. G. Forest, Qi Wang, and Ruhai Zhou, Dimensional Robustness & Instability of Sheared Semi-dilute, Nano-rod Dispersions, Siam Journal on Multiscale Modeling and Simulation, 7 (2008), 622-654.
- 3. T. Y. Zhang, N. Cogan, and Q. Wang, "Phase Field Models for Biofilms. I. Theory and 1-D simulations," Siam Journal on Applied Math, 69 (3) (2008), 641-669.
- 4. J. Lee, M. G. Forest, Q. Wang, and R. Zhou, "Dipole-induced bi-stability and hysteresis in nanorod monolayers," Physics Letters A, 372 (2008), 3484-3487.
- 5. Sarthok Sircar and Qi Wang, Shear induced mesostructures in biaxial liquid crystal polymers, Phys. Rev. E.,, 78 (2008), 061702.
- 6. X. Yang, M. G. Forest, W. Mullins and Q. Wang, Dynamic defect morphology and hydrodynamics of sheared nematic polymers in two space dimensions, *J. of Rheology*, to appear 2008.
- 7. Qingqing Liao, M. G. Forest, and Qi Wang, "2-D Kinetic Theory for Polymer Particulate Nanocomposites," Communication in Computational Physics, to appear 2009.
- 8. X. Yang, M. G. Forest, Q. Wang, W. Mullins, Quench sensitivity to defects and shear banding in nematic polymer film flows, Journal. Non-Newtonain Fluid Mechanics, to appear 2009.
- 9. Jun Li, Sarthok Sircar, and Qi Wang, A Note on the Kinematics of Rigid Molecules in Linear Flow Fields and Kinetic Theory for Biaxial Liquid Crystal Polymers, Electronic-Liquid Crystal Communications, 2009.

#### PAPERS SUBMITTED

- 10. Q. Wang and T. Y. Zhang, "Kinetic theories for Biofilms", submitted to DCDS-B, 2008.
- 11. Jun Li, M. G. Forest, Qi Wang and R Zhou, "Flows of polymer-particulate nanocomposites: weakly semiflexible limit," submitted to Journal of Computational and Theoretical Nanotechnology, 2008.
- 12. Jinsong Hua, Ping Lin, Chun, Liu, Qi Wang, Energy Law Preserving \$C^0\$ Finite Element Schemes for Phase Field Models in Two-phase Flow Computations, submitted to Siam J. Sci. Comp., 2008.
- 13. Xiaofeng Yang, M. Greg Forest, Bill Mullins, and Qi Wang, Tensorial defect diagnostics for nematic polymers, submitted to Nature Materials, 2008.
- 14. Sarthok Sircar and Qi Wang, Dynamics and rheology of ellipsoidal suspensions in shear flows, submitted to Journal of Rheology, 2008.
- 15. Sarthok Sircar and Qi Wang, Dynamics of bent-core liquid crystal polymers in shear flows, submitted to Communications in Mathematical Sciences, 2008.
- L. Nguyen, W. Yang, Q. Wang, and L. Hirst, Molecular dynamics simulation of Factin: Studying the mechanisms for semiflexible filament assembly reveals the role of cross-linkers, submitted to Macromolecules, 2008.
- 17. Jun Li and Qi Wang, "Flow Driven Dynamics of Sheared Flowing Polymer-Particulate Nanocomposites," submitted to Discrete and Conditnuous Dynamical Systems-Series B, 2008.
- 18. Jianyang Liu, George G P Xiang, Q. Wang, "Variational approach to risk-adjusted performance measures," Submitted to Journal of Risk, 2008.
- 19. T. Y. Zhang and Q. Wang, Cahn-Hilliard vs Singular Cahn-Hilliard Equations in Phase Field Modeling, Submitted to CICP, 2008.

## **Books Chapters**

20. Q. Wang, "Introduction to kinetic theory for complex fluids", in a book on Complex Fluids, in the Contemporary Applied Mathematics (CAM) series, edited by P. G. Ciarlet and Tatsien Li, Higher Education Press and World Scientific, 2008.